

ANSWERS TO PROBLEMS

Chapter 1

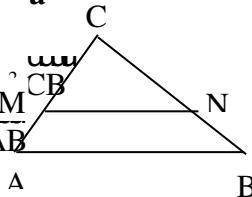
1.2 Problems

1. a. scalar b. scalar c. vector d. neither e. vector f. scalar
 g. scalar h. neither i. scalar j. vector k. vector l. vector

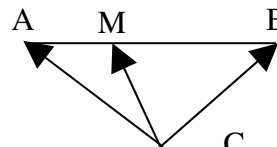
1.3 Problems

1. a. $\mathbf{c} = \mathbf{b} - \mathbf{a}$ b. $\mathbf{c} = \mathbf{a} - \mathbf{b}$ c. $\mathbf{c} = -\mathbf{a} - \mathbf{b}$

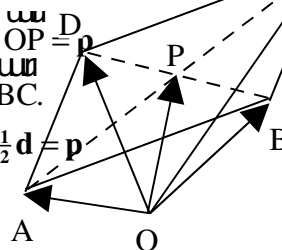
2. a. $\overrightarrow{OC} = \mathbf{a} + \mathbf{b}$ b. $\overrightarrow{AB} = \mathbf{b} - \mathbf{a}$

3.
$$\begin{aligned} \overrightarrow{MN} &= \overrightarrow{MC} + \overrightarrow{CN} = \frac{2}{3}\overrightarrow{AC} + \frac{1}{3}\overrightarrow{CB} \\ &= \frac{2}{3}(\overrightarrow{AC} + \overrightarrow{CB}) = \frac{2}{3}\overrightarrow{AB} \end{aligned}$$


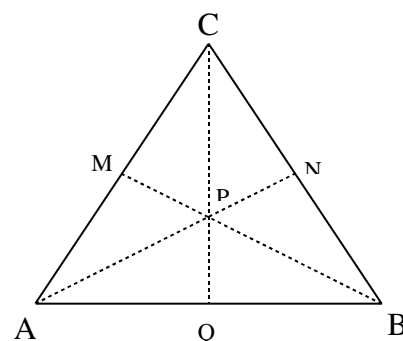
4.
$$\begin{aligned} \overrightarrow{OM} &= \overrightarrow{OA} + \overrightarrow{AM} = \overrightarrow{OA} + t\overrightarrow{AB} \\ &= \overrightarrow{OA} + t(\overrightarrow{AO} + \overrightarrow{OB}) \\ &= (1-t)\overrightarrow{OA} + t\overrightarrow{OB} = s\overrightarrow{OA} + t\overrightarrow{OB} \end{aligned}$$



5. Let $\overrightarrow{OA} = \mathbf{a}$, $\overrightarrow{OB} = \mathbf{b}$, $\overrightarrow{OC} = \mathbf{c}$, $\overrightarrow{OD} = \mathbf{d}$, $\overrightarrow{OP} = \mathbf{p}$.
 Since ABCD is a parallelogram, $\overrightarrow{AD} = \overrightarrow{BC}$.
 Hence $\mathbf{d} - \mathbf{a} = \mathbf{c} - \mathbf{b}$, so $\frac{1}{2}\mathbf{a} + \frac{1}{2}\mathbf{c} = \frac{1}{2}\mathbf{b} + \frac{1}{2}\mathbf{d} = \mathbf{p}$.
 This shows that P bisects AC and BD.



6. Let M and N be the mid points of AC and BC.
 Let P be the intersection of medians AN and BM.



BC.
 BM.

$$\overrightarrow{CP} = (1-s)\overrightarrow{CM} + s\overrightarrow{CB} = (1-s)\left(\frac{1}{2}\overrightarrow{CA}\right) + s\overrightarrow{CB} \quad (1)$$

$$\overrightarrow{CP} = t\overrightarrow{CA} + (1-t)\overrightarrow{CN} = t\overrightarrow{CA} + (1-t)\left(\frac{1}{2}\overrightarrow{CB}\right) \quad (2)$$

Equate (1) & (2).

$$(1-s)\left(\frac{1}{2}\overrightarrow{CA}\right) + s\overrightarrow{CB} = t\overrightarrow{CA} + (1-t)\left(\frac{1}{2}\overrightarrow{CB}\right)$$

$$[(1-s)\left(\frac{1}{2}\right) - t]\overrightarrow{CA} = [(1-t)\left(\frac{1}{2}\right) - s]\overrightarrow{CB}$$

Since $\overrightarrow{CA}, \overrightarrow{CB}$ not parallel, $(1-s)\left(\frac{1}{2}\right) - t = 0$ & $(1-t)\left(\frac{1}{2}\right) - s = 0$.

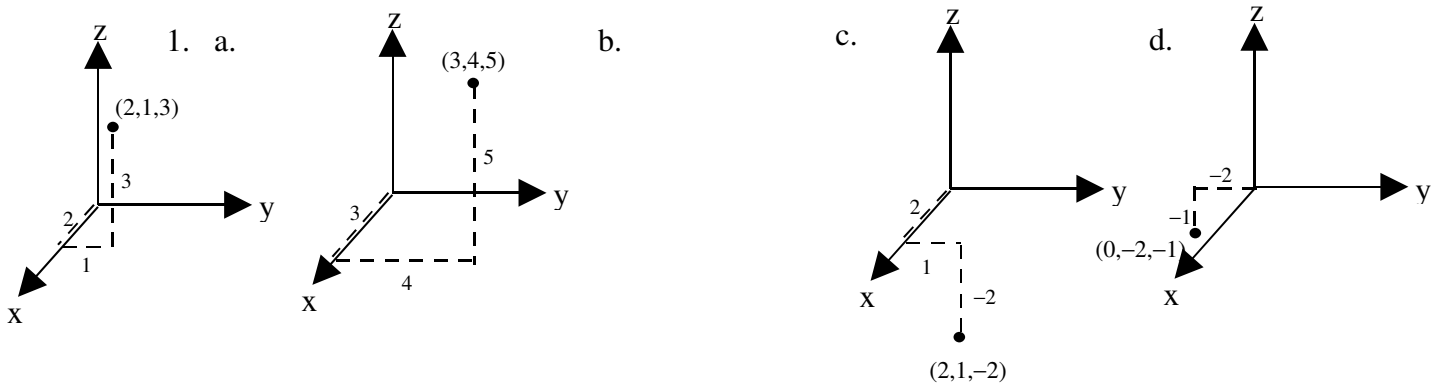
Solving these equations for s, t gives $s = t = \frac{1}{3}$.

$$\text{So } \overrightarrow{CP} = (1-s)\left(\frac{1}{2}\overrightarrow{CA}\right) + s\overrightarrow{CB} = \left(1 - \frac{1}{3}\right)\left(\frac{1}{2}\overrightarrow{CA}\right) + \frac{1}{3}\overrightarrow{CB} = \frac{1}{3}\overrightarrow{CA} + \frac{1}{3}\overrightarrow{CB}.$$

$$\text{Let } Q \text{ be the mid point of } AB. \text{ Then } \overrightarrow{CQ} = \frac{1}{2}\overrightarrow{CA} + \frac{1}{2}\overrightarrow{CB} = \frac{3}{2}\left(\frac{1}{3}\overrightarrow{CA} + \frac{1}{3}\overrightarrow{CB}\right) = \frac{3}{2}\overrightarrow{CP}.$$

This shows that \overrightarrow{CP} is parallel to \overrightarrow{CQ} so P lies on CQ . Hence the medians are concurrent.

1.4 Problems



2. $(1,0,0), (1,1,0), (0,1,0), (1,0,1), (0,1,1), (0,0,1)$

3. $(2,0,0), (2,3,0), (0,3,0), (0,0,1), (2,0,1), (0,3,1)$

4. $(2,0,0), (0,2,0), (1,1,2)$

5. $(\sqrt{3}/2, 1/2, 0), (\sqrt{3}/6, 1/2, \sqrt{2}/\sqrt{3})$

1.5 Problems

1. a. $(5, 2, 1)$ b. $(-1, 0, 5)$ c. $(8, -2, 2)$ d. $(-5, -1, 12)$ e. $(-4, 6, -4)$ f. $(9, 6, -1)$

2. a. $\sqrt{14}$ b. $\sqrt{14}$ c. $6\sqrt{2}$ d. $\sqrt{30}$ e. $\sqrt{26}$ f. $\sqrt{14}$
3. a. (1, 2, 4) b. (2, 6, -3) c. (6, -8, 1) d. (2, -3, 3)
4. a. $B = (4, 8, 6)$ b. $B = (3, 3, 6)$
5. a. $A = (-1, 0, 2)$ b. $A = (2, -4, 3)$
6. a. $\pm(2/3, 2/3, 1/3)$ b. $\pm(3/5, 0, 4/5)$ c. $\pm(1/\sqrt{14}, 2/\sqrt{14}, 3/\sqrt{14})$
d. $\pm(-2/\sqrt{29}, 3/\sqrt{29}, -4/\sqrt{29})$
7. $\pm\sqrt{2}$

1.6 Problems

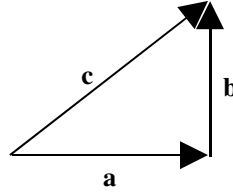
1. a. 11 b. 2 c. 13 d. 13 e. 28
2. a. $\sqrt{6}$ b. $\sqrt{29}$ c. $\sqrt{11}$ d. $\sqrt{57}$ e. $\sqrt{153}$
3. a. $11/\sqrt{174}$ b. $2/\sqrt{66}$ c. $13/\sqrt{319}$ d. $-23/\sqrt{741}$
4. a. $(2, 1, 3) \bullet (1, 1, -1) = (2)(1) + (1)(1) + (3)(-1) = 2 + 1 - 3 = 0$
b. $(1, 3, 5) \bullet (2, 1, -1) = (1)(2) + (3)(1) + (5)(-1) = 2 + 3 - 5 = 0$
c. $(4, 5, 1) \bullet (2, -1, -3) = (4)(2) + (5)(1) + (1)(-3) = 8 - 5 - 3 = 0$
d. $(1, 0, 1) \bullet (0, 1, 0) = (1)(0) + (0)(1) + (1)(0) = 0 + 0 + 0 = 0$
5. a. (2, 3) b. (1, -2) c. (3, 1) d. (1, 3)
6. a. $(3/2, 1/2, 0)$ b. $(13/9, 26/9, 26/9)$ c. (6, 2, 2) d. $(27/26, 18/13, 9/26)$
7. a. $17/5$ b. $9/5$ c. $60/13$ d. $8/\sqrt{5}$

8. $\mathbf{c} = \mathbf{a} + \mathbf{b} \Rightarrow \mathbf{c} \cdot \mathbf{c} = (\mathbf{a} + \mathbf{b}) \cdot (\mathbf{a} + \mathbf{b}) \Rightarrow$

$$\mathbf{c} \cdot \mathbf{c} = \mathbf{a} \cdot \mathbf{a} + \mathbf{a} \cdot \mathbf{b} + \mathbf{b} \cdot \mathbf{a} + \mathbf{b} \cdot \mathbf{b} \Rightarrow$$

$$\|\mathbf{c}\|^2 = \|\mathbf{a}\|^2 + 0 + 0 + \|\mathbf{b}\|^2 \Rightarrow$$

$$\|\mathbf{c}\|^2 = \|\mathbf{a}\|^2 + \|\mathbf{b}\|^2$$

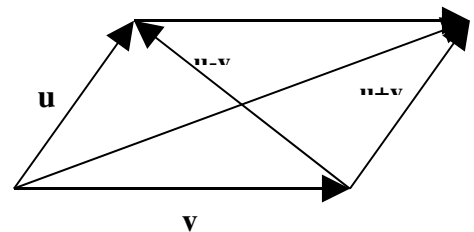
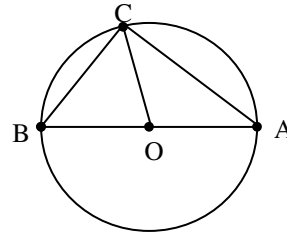


9. Let $\vec{OA} = \mathbf{a}$ and $\vec{OC} = \mathbf{c}$. Then

$$\vec{BC} \cdot \vec{AC} = (\mathbf{a} + \mathbf{c}) \cdot (\mathbf{c} - \mathbf{a})$$

$$= \mathbf{a} \cdot \mathbf{c} - \mathbf{a} \cdot \mathbf{a} + \mathbf{c} \cdot \mathbf{c} - \mathbf{c} \cdot \mathbf{a}$$

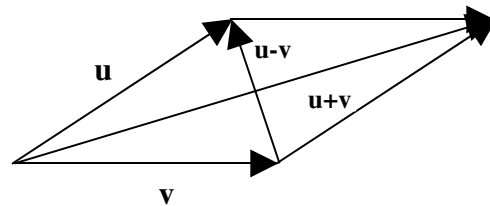
$$= -\|\mathbf{a}\|^2 + \|\mathbf{c}\|^2 = 0 \text{ since } \|\mathbf{a}\| = \|\mathbf{c}\| \text{ and } \mathbf{a} \perp \mathbf{c}$$



10. $\|\mathbf{u} + \mathbf{v}\|^2 + \|\mathbf{u} - \mathbf{v}\|^2 = (\mathbf{u} + \mathbf{v}) \cdot (\mathbf{u} + \mathbf{v}) + (\mathbf{u} - \mathbf{v}) \cdot (\mathbf{u} - \mathbf{v})$

$$= \mathbf{u} \cdot \mathbf{u} + \mathbf{u} \cdot \mathbf{v} + \mathbf{v} \cdot \mathbf{u} + \mathbf{v} \cdot \mathbf{v} + \mathbf{u} \cdot \mathbf{u} - \mathbf{u} \cdot \mathbf{v} - \mathbf{v} \cdot \mathbf{u} + \mathbf{v} \cdot \mathbf{v}$$

$$= 2\mathbf{u} \cdot \mathbf{u} + 2\mathbf{v} \cdot \mathbf{v} = 2\|\mathbf{u}\|^2 + 2\|\mathbf{v}\|^2 = \|\mathbf{u}\|^2 + \|\mathbf{u}\|^2 + \|\mathbf{v}\|^2 + \|\mathbf{v}\|^2$$



11. $(\mathbf{u} + \mathbf{v}) \cdot (\mathbf{u} - \mathbf{v}) = \mathbf{u} \cdot \mathbf{u} - \mathbf{u} \cdot \mathbf{v} + \mathbf{v} \cdot \mathbf{u} - \mathbf{v} \cdot \mathbf{v}$

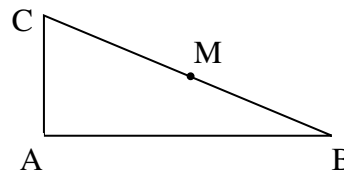
$$= \mathbf{u} \cdot \mathbf{u} - \mathbf{v} \cdot \mathbf{v} = \|\mathbf{u}\|^2 - \|\mathbf{v}\|^2 = 0 \text{ since } \|\mathbf{u}\| = \|\mathbf{v}\|$$

12. Let ABC be rt. Δ with hypotenuse BC. Let M be the

mid point of BC. Then

$$\|\vec{BM}\| = \|\vec{CM}\| = \frac{1}{2} \|\vec{BC}\|. \text{ We must show}$$

$$\|\vec{AM}\| = \frac{1}{2} \|\vec{BC}\|. \text{ Now}$$



$$\|\vec{AM}\|^2 = \vec{AM} \cdot \vec{AM} = \left(\frac{1}{2} \vec{AB} + \frac{1}{2} \vec{AC}\right) \cdot \left(\frac{1}{2} \vec{AB} + \frac{1}{2} \vec{AC}\right)$$

$$= \frac{1}{4} \vec{AB} \cdot \vec{AB} + \frac{1}{4} \vec{AB} \cdot \vec{AC} + \frac{1}{4} \vec{AC} \cdot \vec{AB} + \frac{1}{4} \vec{AC} \cdot \vec{AC}$$

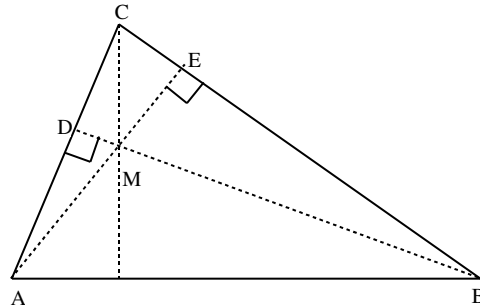
$$= \frac{1}{4} \|\vec{AB}\|^2 + 0 + 0 + \frac{1}{4} \|\vec{AC}\|^2 \quad (\vec{AB} \perp \vec{AC}; \therefore \vec{AB} \cdot \vec{AC} = 0)$$

$$= \frac{1}{4} (\|\vec{AB}\|^2 + \|\vec{AC}\|^2) = \frac{1}{4} \|\vec{BC}\|^2 \quad (\text{using pythagoras' theorem})$$

Since $\|\vec{AM}\|^2 = \frac{1}{4} \|\vec{BC}\|^2$, taking square roots gives $\|\vec{AM}\| = \frac{1}{2} \|\vec{BC}\|$ as required.

13. Let AE and BD be altitudes of $\triangle ABC$. Let altitudes AE and BD intersect at M. We must show $CM \perp AB$ or

$$\vec{CM} \cdot \vec{AB} = 0. \quad \text{Now}$$



$$\begin{aligned} \vec{CM} \cdot \vec{AB} &= \vec{CM} \cdot (\vec{AM} + \vec{MB}) = \vec{CM} \cdot \vec{AM} + \vec{CM} \cdot \vec{MB} \\ &= (\vec{CB} + \vec{BM}) \cdot \vec{AM} + (\vec{CA} + \vec{AM}) \cdot \vec{MB} \\ &= \vec{CB} \cdot \vec{AM} + \vec{BM} \cdot \vec{AM} + \vec{CA} \cdot \vec{MB} + \vec{AM} \cdot \vec{MB} \\ &= \mathbf{0} + \vec{BM} \cdot \vec{AM} + \mathbf{0} + \vec{AM} \cdot \vec{MB} = \vec{AM} \cdot (\vec{BM} + \vec{MB}) \\ &= \vec{AM} \cdot (\vec{BM} - \vec{BM}) = \vec{AM} \cdot \mathbf{0} = 0 \end{aligned}$$

14. a. $\mathbf{i} \cdot \mathbf{i} = (1,0) \cdot (1,0) = 1 \quad \mathbf{i} \cdot \mathbf{j} = (1,0) \cdot (0,1) = 0$

b. $\mathbf{a} = \vec{OA} = \vec{OY} + \vec{YA} = \cos \alpha \mathbf{i} + \sin \alpha \mathbf{j}$

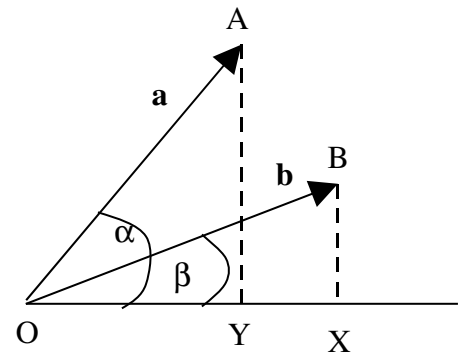
$$\mathbf{b} = \vec{OB} = \vec{OX} + \vec{XB} = \cos \beta \mathbf{i} + \sin \beta \mathbf{j}$$

c. $\mathbf{a} \cdot \mathbf{b} = \|\mathbf{a}\| \|\mathbf{b}\| \cos(\alpha - \beta) = 1 \cdot 1 \cdot \cos(\alpha - \beta) = \cos(\alpha - \beta)$

$$\begin{aligned} \text{But } \mathbf{a} \cdot \mathbf{b} &= (\cos \alpha \mathbf{i} + \sin \alpha \mathbf{j}) \cdot (\cos \beta \mathbf{i} + \sin \beta \mathbf{j}) \\ &= \cos \alpha \cos \beta + \sin \alpha \sin \beta \end{aligned}$$

Equating the two expressions for $\mathbf{a} \cdot \mathbf{b}$ gives

$$\cos(\alpha - \beta) = \cos \alpha \cos \beta + \sin \alpha \sin \beta$$



1.6 Problems

1. a. $(7, -2, 11)$ b. $(10, -12, -2)$ c. $(1, -14, 3)$ d. $(17, -14, -13)$

2. a. $(37, -10, -59)$ b. $(3, -50, 11)$ c. 0

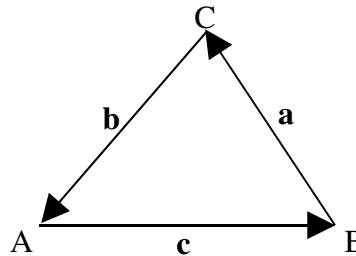
3. a. $(7, -2, -11)$ b. $(10, -12, -2)$

4. a. $\sqrt{174}$ b. $2\sqrt{62}$ c. $\sqrt{206}$

5. a. $\sqrt{174}/2$ b. $\sqrt{62}$ c. $\sqrt{206}/2$

6. a. $\sqrt{26}/2$ b. $5\sqrt{5}/2$

7. $\mathbf{a} + \mathbf{b} + \mathbf{c} = \mathbf{0} \Rightarrow \mathbf{a} \times (\mathbf{a} + \mathbf{b} + \mathbf{c}) = \mathbf{a} \times \mathbf{0} \Rightarrow$
 $\mathbf{a} \times \mathbf{a} + \mathbf{a} \times \mathbf{b} + \mathbf{a} \times \mathbf{c} = \mathbf{0}$. But $\mathbf{a} \times \mathbf{a} = \mathbf{0} \Rightarrow$
 $\mathbf{a} \times \mathbf{b} = -\mathbf{a} \times \mathbf{c} \Rightarrow \mathbf{a} \times \mathbf{b} = \mathbf{c} \times \mathbf{a} \Rightarrow$
 $\|\mathbf{a}\| \cdot \|\mathbf{b}\| \cdot \sin C = \|\mathbf{c}\| \cdot \|\mathbf{a}\| \cdot \sin B \Rightarrow$
 $\frac{\sin C}{\|\mathbf{c}\|} = \frac{\sin B}{\|\mathbf{b}\|}$. Similarly $\frac{\sin B}{\|\mathbf{b}\|} = \frac{\sin A}{\|\mathbf{a}\|}$



8. a. \mathbf{u} parallel to $\mathbf{v} \Rightarrow \mathbf{v} = k\mathbf{u} \Rightarrow \mathbf{v} = (ku_1, ku_2, ku_3)$

$$\begin{aligned} \mathbf{u} \times \mathbf{v} &= \left(\begin{vmatrix} u_2 & u_3 \\ ku_2 & ku_3 \end{vmatrix}, -\begin{vmatrix} u_1 & u_3 \\ ku_1 & ku_3 \end{vmatrix}, \begin{vmatrix} u_1 & u_2 \\ ku_1 & ku_2 \end{vmatrix} \right) \\ &= (u_2ku_3 - u_3ku_2, -u_1ku_3 + u_3ku_1, u_1ku_2 - u_2ku_1) \\ &= (0, 0, 0) = \mathbf{0}. \end{aligned}$$

b. $\mathbf{u} \times \mathbf{v} = \mathbf{0} \Rightarrow \|\mathbf{u}\| \|\mathbf{v}\| \sin \theta = 0 \Rightarrow \sin \theta = 0 \Rightarrow \theta = 0$.

1.8 Problems

1. a. $4\mathbf{i}+3\mathbf{j}+7\mathbf{k}$ b. $3\mathbf{i}-\mathbf{j}+2\mathbf{k}$ c. $-2\mathbf{i}+5\mathbf{j}+6\mathbf{k}$ d. $\mathbf{i}+2\mathbf{k}$

2. a. $\mathbf{i} \bullet \mathbf{i} = (1, 0, 0) \bullet (1, 0, 0) = (1)(1) + (0)(0) + (0)(0) = 1 + 0 + 0 = 1$

b. $\mathbf{j} \bullet \mathbf{j} = (0, 1, 0) \bullet (0, 1, 0) = (0)(0) + (1)(1) + (0)(0) = 0 + 1 + 0 = 1$

c. $\mathbf{i} \bullet \mathbf{j} = (1, 0, 0) \bullet (0, 1, 0) = (1)(0) + (0)(1) + (0)(0) = 0 + 0 + 0 = 0$

d. $\mathbf{j} \bullet \mathbf{k} = (0, 1, 0) \bullet (0, 0, 1) = (0)(0) + (1)(0) + (0)(1) = 0 + 0 + 0 = 0$

e. $\mathbf{i} \times \mathbf{i} = (1, 0, 0) \times (1, 0, 0) = \left(\begin{vmatrix} 0 & 0 \\ 0 & 0 \end{vmatrix}, -\begin{vmatrix} 1 & 0 \\ 1 & 0 \end{vmatrix}, \begin{vmatrix} 1 & 0 \\ 1 & 0 \end{vmatrix} \right) = (0, 0, 0) = \mathbf{0}$

f. $\mathbf{i} \times \mathbf{j} = (1, 0, 0) \times (0, 1, 0) = \left(\begin{vmatrix} 0 & 0 \\ 1 & 0 \end{vmatrix}, -\begin{vmatrix} 1 & 0 \\ 0 & 0 \end{vmatrix}, \begin{vmatrix} 1 & 0 \\ 0 & 1 \end{vmatrix} \right) = (0, 0, 1) = \mathbf{k}$

g. $\mathbf{i} \times \mathbf{k} = (1, 0, 0) \times (0, 0, 1) = \left(\begin{vmatrix} 0 & 0 \\ 0 & 1 \end{vmatrix}, -\begin{vmatrix} 1 & 0 \\ 0 & 1 \end{vmatrix}, \begin{vmatrix} 1 & 0 \\ 0 & 0 \end{vmatrix} \right) = (0, -1, 0) = -(0, 1, 0) = -\mathbf{j}$

h. $\mathbf{j} \times \mathbf{k} = (0, 1, 0) \times (0, 0, 1) = \left(\begin{vmatrix} 1 & 0 \\ 0 & 1 \end{vmatrix}, -\begin{vmatrix} 0 & 0 \\ 0 & 1 \end{vmatrix}, \begin{vmatrix} 0 & 1 \\ 0 & 0 \end{vmatrix} \right) = (1, 0, 0) = \mathbf{i}$

3. a. $6 - 6 + 5 = 5$ b. $6 - 5 + 24 = 25$ c. $8 - 10 - 9 = -11$ d. $6 - 3 - 6 = -3$

4. a. $\left(\begin{vmatrix} 3 & 1 \\ -1 & 5 \end{vmatrix}, -\begin{vmatrix} 2 & 1 \\ 3 & 5 \end{vmatrix}, \begin{vmatrix} 2 & 3 \\ 3 & -2 \end{vmatrix} \right) = (17, -7, -13) = 17\mathbf{i} - 7\mathbf{j} - 13\mathbf{k}$

b. $\left(\begin{vmatrix} 1 & 4 \\ -5 & 6 \end{vmatrix}, -\begin{vmatrix} 3 & 4 \\ 2 & 6 \end{vmatrix}, \begin{vmatrix} 3 & 1 \\ 2 & -5 \end{vmatrix} \right) = (26, -10, -17) = 26\mathbf{i} - 10\mathbf{j} - 17\mathbf{k}$

$$c. \left(\begin{vmatrix} -5 & 3 \\ 2 & -3 \end{vmatrix}, -\begin{vmatrix} 2 & 3 \\ 4 & -3 \end{vmatrix}, \begin{vmatrix} 2 & -5 \\ 4 & 2 \end{vmatrix} \right) = (9, 18, 24) = 9\mathbf{i} + 18\mathbf{j} + 24\mathbf{k}$$

$$d. \left(\begin{vmatrix} -3 & 2 \\ 1 & -3 \end{vmatrix}, -\begin{vmatrix} 1 & 2 \\ 6 & -3 \end{vmatrix}, \begin{vmatrix} 1 & -3 \\ 6 & 1 \end{vmatrix} \right) = (7, 15, 19) = 7\mathbf{i} + 15\mathbf{j} + 19\mathbf{k}$$

$$5. \quad a. \quad a - 6a - 5 = 0 \Rightarrow -5a = 5 \Rightarrow a = -1 \quad b. \quad 6a - 12 - 3a = 0 \Rightarrow 3a = 12 \Rightarrow a = 4$$

1.9 Problems

$$1. \quad a. \quad (6, 6, 2, 5) \quad b. \quad (-13, -3, 4, 5) \quad c. \quad (3, 4, 3, 1)$$

$$2. \quad a. \quad 18 \quad b. \quad 25 \quad c. \quad 41$$

$$3. \quad a. \quad \sqrt{30} \quad b. \quad \sqrt{115} \quad c. \quad \sqrt{29}$$

$$4. \quad a. \quad (1/\sqrt{30}, 3/\sqrt{30}, 2/\sqrt{30}, 4/\sqrt{30}) \quad b. \quad \frac{1}{\sqrt{35}}(5, 3, 0, 1) \quad c. \quad \frac{1}{\sqrt{30}}(3, 2, -1, 4)$$

$$5. \quad a. \quad (1, 2, 3, 1) \bullet (3, 1, 1, -8) = (1)(3) + (2)(1) + (3)(1) + (1)(-8) = 3 + 2 + 3 - 8 = 0$$

b. c. d. similar to a. as shown above.

$$6. \quad a. \quad (1, 1, 0, 0) \bullet (1, -1, 2, 3) = (1)(1) + (1)(-1) + (0)(2) + (0)(3) = 1 - 1 + 0 + 0 = 0$$

$$(1, 1, 0, 0) \bullet (2, -2, 1, -2) = (1)(2) + (1)(-2) + (0)(1) + (0)(-2) = 2 - 2 + 0 + 0 = 0$$

$$(1, -1, 2, 3) \bullet (2, -2, 1, -2) = (1)(2) + (-1)(-2) + (2)(1) + (3)(-2) = 2 + 2 + 2 - 6 = 0$$

b. c. d. similar to a. as shown above.

Chapter 2

2.2 Problems

$$1. \quad a. \quad (2, 3, 4) \quad b. \quad (1, 3, -2) \quad c. \quad (3, 0, 5)$$

2. a. $(3,2,3) \cdot (x-1, y-0, z-1) = (0, 0, 0)$ b. $(1,2,3) \cdot (x-2, y-2, z-2) = (0, 0, 0)$
 c. $(5,2,-3) \cdot (x-1, y-1, z-0) = (0,0,0)$
3. a. $2x+3y+z=23$ b. $5x+2y+3z=28$ c. $x+z=8$ d. $2x-y+3z=-4$
4. a. $2x+y-z=1$ b. $5x-y+6z=43$ c. $x+2y+z=2$ d. $2x-2y-z=2$

2.3 Problems

1. a. $\mathbf{x} = (1,2,3) + t(2,1,4)$ $x = 1 + 2t$, $y = 2 + t$, $z = 3 + 4t$
 b. $\mathbf{x} = (3,1,3) + t(4,2,5)$ $x = 3 + 4t$, $y = 1 + 2t$, $z = 3 + 5t$
 c. $\mathbf{x} = (4,1,5) + t(1,0,3)$ $x = 4 + t$, $y = 1 + 0t$, $z = 5 + 3t$
 d. $\mathbf{x} = (1,-2,2) + t(2,3,-1)$ $x = 1 + 2t$, $y = -2 + 3t$, $z = 2 - t$
 e. $\mathbf{x} = (2,0,-1) + t(1,-2,3)$ $x = 2 + t$, $y = 0 - 2t$, $z = -1 + 3t$
 f. $\mathbf{x} = (-3,2,0) + t(0,-1,3)$ $x = -3$, $y = 2 - t$, $z = 3t$
2. a. $x = 1 + t$, $y = 3 + 2t$, $z = 4 - 3t$ b. $x = 4 - 2t$, $y = 3 - t$, $z = -1 + 4t$
 c. $x = 2 - t$, $y = -1 + t$, $z = -3 + t$ d. $x = 5 - 4t$, $y = 1 - 2t$, $z = 3 - t$
 e. $x = 4 - 3t$, $y = 3t$, $z = -5 + t$ f. $x = 2 + t$, $y = 2 - 5t$, $z = -2 + 2t$
3. a. $\frac{x-1}{1} = \frac{y-3}{2} = \frac{z-4}{-3}$ b. $\frac{x-4}{-2} = \frac{y-3}{-1} = \frac{z+1}{4}$

$$\text{c. } \frac{x-2}{-1} = \frac{y+1}{1} = \frac{z+3}{1} \quad \text{d. } \frac{x-5}{-4} = \frac{y-1}{-2} = \frac{z-3}{-1}$$

$$\text{e. } \frac{x-4}{-3} = \frac{y-0}{3} = \frac{z+5}{1} \quad \text{f. } \frac{x-2}{1} = \frac{y-2}{-5} = \frac{z+2}{2}$$

2.4 Problems

1. a. 90° b. 60° c. 60° d. 30° e. 45° f. 45°

2. a. $-17/\sqrt{231}$ b. $15/2\sqrt{105}$ c. $14/3\sqrt{22}$ d. $\sqrt{15}/7$

2.5 Problems

1. a. 3 b. $37/5\sqrt{2}$ c. 1 d. 0

2. a. $5/3$ b. $16/\sqrt{11}$

3. a. $\sqrt{13}/\sqrt{22}$ b. $10/\sqrt{3}$ c. $\sqrt{14}$ d. $\sqrt{21}$

4. a. $2/\sqrt{51}$ b. $8/\sqrt{83}$ c. 0 d. $8/\sqrt{510}$

5. a. $1/\sqrt{3}$ b. $10/\sqrt{17}$ c. $13/\sqrt{35}$

2.6 Problems

1. a. $x = \frac{6}{5} - t, y = \frac{7}{5} - 7t, z = 0 - 5t$ b. $x = 0 + 4t, y = 1 - 7t, z = 1 - 2t$
 c. $x = 1 + 3t, y = 2 - 7t, z = 0 + 2t$ d. $x = 0 + 4t, y = \frac{3}{2} + 2t, z = \frac{11}{4} - t$
 e. $x = 2 + t, y = 1 + 4t, z = 3 + 7t$ f. $x = \frac{9}{5} + 4t, y = \frac{7}{5} + 4t, z = 0 - 5t$
2. a. (3, 2, 1) b. (2, 2, 1) c. (-3, 4, -5) d. (1, 4, 1)
3. a. (3, 2, 1) b. (0, 1, 1) c. (3, 0, 2) d. do not intersect.

2.7 Problems

1. a. (2, 3, 1) $\left(\frac{2}{\sqrt{14}}, \frac{3}{\sqrt{14}}, \frac{1}{\sqrt{14}} \right)$ b. (4, 1, 1) $\left(\frac{4}{3\sqrt{2}}, \frac{1}{3\sqrt{2}}, \frac{1}{3\sqrt{2}} \right)$
 c. (1, 2, 3) $\left(\frac{1}{\sqrt{14}}, \frac{2}{\sqrt{14}}, \frac{3}{\sqrt{14}} \right)$ d. (1, 3, 5)
 $\left(\frac{1}{\sqrt{35}}, \frac{3}{\sqrt{35}}, \frac{5}{\sqrt{35}} \right)$
2. a. (1, -3, 4) $\left(\frac{1}{\sqrt{26}}, -\frac{3}{\sqrt{26}}, \frac{4}{\sqrt{26}} \right)$ b. (-1, 2, 0) $\left(-\frac{1}{\sqrt{5}}, \frac{2}{\sqrt{5}}, 0 \right)$
 c. (4, 2, 3) $\left(\frac{4}{\sqrt{29}}, \frac{2}{\sqrt{29}}, \frac{3}{\sqrt{29}} \right)$ d. (3, 0, -4) $\left(\frac{3}{5}, 0, -\frac{4}{5} \right)$
3. a. $x = 2 + 3t, y = 5 + 2t, z = 1 + 4t$ b. $x = 3 - t, y = -2, z = 1 + 2t$
 c. $x = 4 + 3t, y = 1, z = 3 + 2t$ d. $x = 5 + 2t, y = t, z = -2 - 2t$
4. a. $3x + 2y + 4z = 20$ b. $x - 2z = 1$ c. $3x + 2z = 18$ d. $2x + y - 2z = 6$