MATH 2130 Tutorial 12

- **1.** Find the area bounded by $(x^2 + y^2)^3 = 4a^2x^2y^2$.
- **2.** Find the double integral of f(x, y) = xy(x + y) over the region in the first quadrant bounded by $x^2 + y^2 = 1$ and $x^2 + y^2 = 4$.
- **3.** Evaluate the triple integral of the function f(x, y, z) = x over the volume bounded by the surfaces

$$2x + 3y + z = 6$$
, $x = 0$, $y = 0$, $z = 0$.

4. Find the volume in the first octant bounded by the surfaces

$$4x + 4y + z = 16$$
, $z = 0$, $y = x/2$, $y = 2x$

5. Set up, but do **NOT** evaluate, a triple iterated integral for the volume in the first octant bounded by the surfaces

$$z = 2x + y$$
, $9x^2 + 4y^2 = 1$, $x = 0$, $y = 0$, $z = 0$.

6. Set up, but do **NOT** evaluate, a triple iterated integral for the volume bounded by the surfaces

$$z = 9 - x^2 - y^2$$
, $z = x^2$.

7. Find the volume bounded by the surfaces

$$z = xy, \quad x^2 + y^2 = 1, \quad z = 0.$$

8. Find the volume bounded by the surfaces

$$z = 2\sqrt{x^2 + y^2}$$
 and $z = 9 - x^2 - y^2$.

Get a numerical answer, but do not simplify it.

9. Set up, but do **NOT** evaluate, a triple iterated integral for the triple integral of the function $f(x, y, z) = x^2 + y^3$ over the volume bounded by the surfaces

$$(x^2 + y^2)^2 = 2xy, \quad z = \sqrt{1 - x^2 - y^2}, \quad z = 0.$$

Answers 1. $\pi a^2/2$ 2. 62/15 3. 9/2 4. 128/95. $\int_0^{1/3} \int_0^{(1/2)\sqrt{1-9x^2}} \int_0^{2x+y} dz \, dy \, dx$ 6. $4 \int_0^{3/\sqrt{2}} \int_0^{\sqrt{9-2x^2}} \int_{x^2}^{9-x^2-y^2} dz \, dy \, dx$ 7. 1/2 8. $2\pi \left[\frac{9(\sqrt{10}-1)^2}{2} - \frac{(\sqrt{10}-1)^4}{4} - \frac{2(\sqrt{10}-1)^3}{3} \right]$ 9. $2 \int_0^{\pi/2} \int_0^{\sqrt{\sin 2\theta}} \int_0^{\sqrt{1-r^2}} r^3 \cos^2 \theta \, dz \, dr \, d\theta$