

The Golden Ratio

Given a line segment AB , the point C on the line such that the ratio of the length of the line AB to the length AC is the same as the ratio of the length of line segment AC to the length CB .



This ratio is known as the golden ratio and is denoted by the greek letter ϕ . $\frac{AB}{AC} = \frac{AC}{CB} = \phi$

The Golden Ratio: $\frac{AB}{AC} = \frac{AC}{CB} = \phi$



Golden Ratio: Solutions to quadratic equations

An equation of the form:

$$ax^2 + bx + c = 0$$

has solutions

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

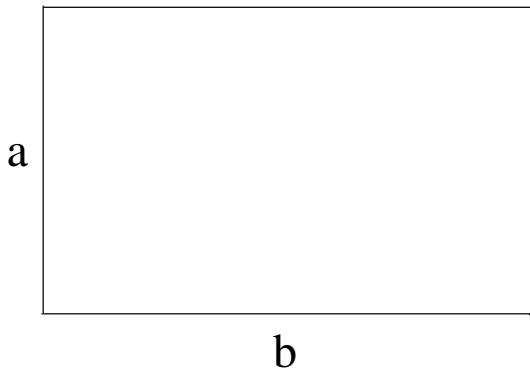
The value of the Golden Ratio

Construction 1: The Golden Cut



Golden Rectangle

A Golden rectangle is a rectangle that has side lengths that are in golden proportion.

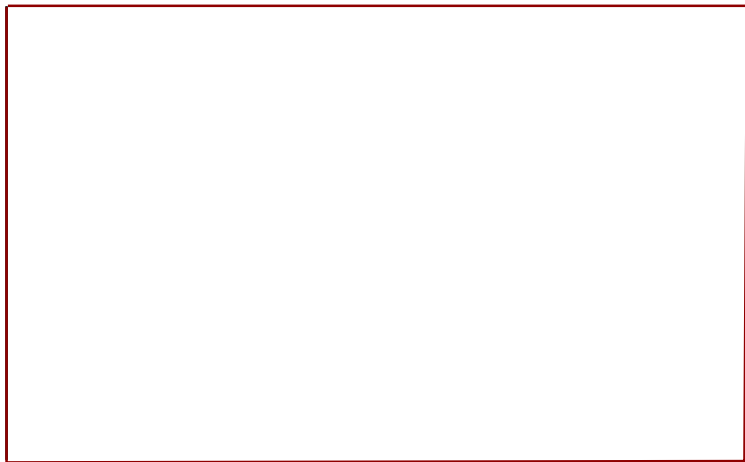


$$\frac{b}{a} = \phi$$

Construction 2: Golden Rectangle given shorter side

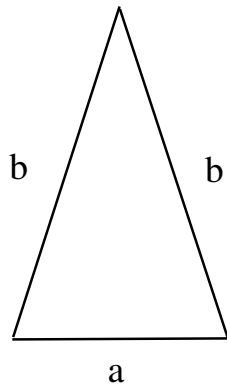


Construction 3: Golden Spiral



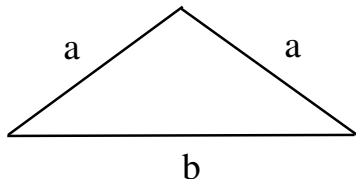
Golden Triangles

Golden Acute Triangle

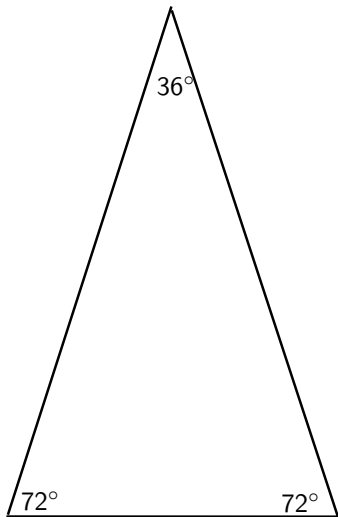


$$\frac{b}{a} = \phi$$

Golden Obtuse Triangle



Is this a Golden Acute Triangle?



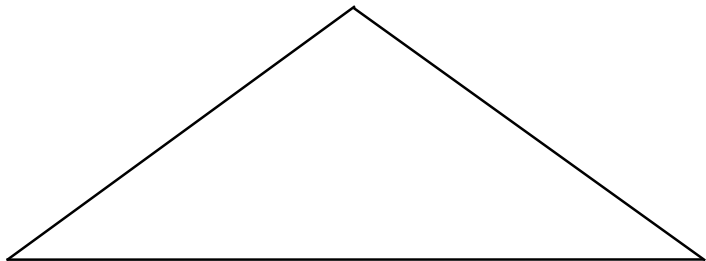
Construction 4: Acute Golden Triangle over a given base



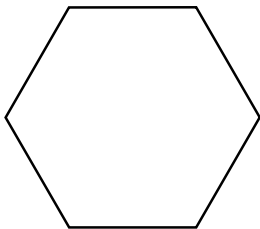
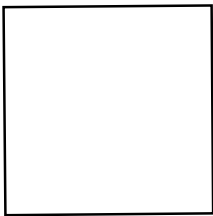
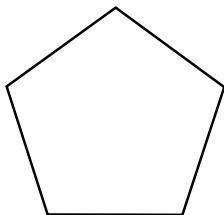
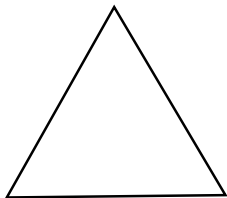
Construction 5: Acute Golden Triangle over a given base alternate construction



Construction 6: Subdividing an Obtuse Golden Triangle



Regular Polygons



Construction 7: Regular Pentagon over a given side

