

Math 1010 Assignment 1 Solutions Summer 2014

1. (a)

$$\begin{aligned}12\left(\frac{2x}{3}\right) + (12)3(x-1) &= (12)\frac{5(1-2x)}{4} + 12(2x) \\8x + 36(x-1) &= 15(1-2x) + 24x \\8x + 36x - 36 &= 15 - 30x + 24x \\44x + 6x &= 15 + 36 \\50x &= 51 \\x &= \frac{51}{50}\end{aligned}$$

(b)

$$\begin{aligned}4(x-1) + 3x &= 7x + 24 \\4x - 4 + 3x &= 7x + 24 \\7x - 7x &= 24 + 4 \\0 &= 28\end{aligned}$$

The equation has no solutions.

(c)

$$\begin{aligned}2(1-4y) + 3y + 2 &= -5y + 4 \\2 - 8y + 3y + 2 &= -5y + 4 \\-5y + 5y &= 4 - 4 \\0 &= 0\end{aligned}$$

All real numbers satisfy the equation.

2. (a)

$$\begin{aligned}6\left(\frac{5x}{2}\right) + (6)2(3+x) &\geq (6)\frac{4(x-5)}{3} \\15x + 12(3+x) &\geq 8(x-5) \\15x + 36 + 12x &\geq 8x - 40 \\27x - 8x &\geq -40 - 36 \\19x &\geq -76 \\x &\geq -\frac{76}{19} \\x &\geq -4\end{aligned}$$

(b)

$$\begin{aligned}3(x-5) - x + 10 &\geq 2x + 6 \\3x - 15 - x + 10 &\geq 2x + 6 \\2x - 2x &\geq 6 + 5 \\0 &\geq 11\end{aligned}$$

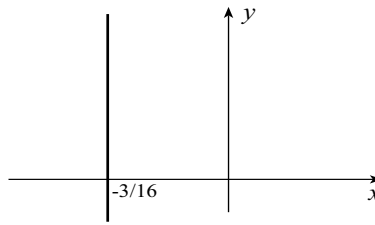
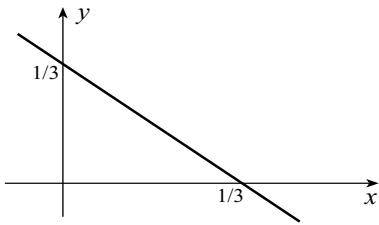
The inequality has no solutions.

(c)

$$\begin{aligned}10y + 3(4 - 2y) &< 2y + 2(y + 15) \\10y + 12 - 6y &< 2y + 2y + 30 \\4y - 4y &< 30 - 12 \\0 &< 18\end{aligned}$$

All real numbers satisfy the inequality.

3. (a) Because of the term  $2y^2$ , this equation does not represent a straight line.  
(b) Because the square root is above the  $x$ , this equation does not represent a straight line.  
(c) This is a straight line. It is shown in the left figure below.



(d) This is the equation of a straight line. To draw it, we rewrite the equation in the form

$$3(1 - 5x) = 3(2) + 3\left(\frac{x}{3}\right) \implies 3 - 15x = 6 + x \implies -16x = 3 \implies x = -\frac{3}{16}.$$

It is shown in the right figure above.

4. When we write the equation of the given line in the form  $y = \frac{5}{6}x + \frac{777}{6}$ , we see that its slope is the  $5/6$ . The slope of the required line is therefore  $-6/5$ . Its equation is

$$\begin{aligned}y + 3 &= -\frac{6}{5}(x - 2) \\5(y + 3) &= -6(x - 2) \\5y + 15 - 6x + 12 & \\6x + 5y &= -3\end{aligned}$$

5. When we write the equation of the given line in the form  $y = -\frac{3}{2}x - 36$ , we see that its slope is the  $-3/2$ . The slope of the required line is therefore  $-3/2$  also. To find the point of intersection of the lines  $6x - 4y = -11$  and  $x = 2y$ , we substitute  $x = 2y$  in the first equation

$$6(2y) - 4y = -11 \implies 12y - 4y = -11 \implies 8y = -11 \implies y = -\frac{11}{8}.$$

This gives  $x = -11/4$ . The point of intersection is therefore  $(-11/4, -11/8)$ . The equation of the required line is therefore

$$\begin{aligned}y + \frac{11}{8} &= -\frac{3}{2}\left(x + \frac{11}{4}\right) \\8(y) + 8\left(\frac{11}{8}\right) &= 8\left[-\frac{3}{2}\left(x + \frac{11}{4}\right)\right] \\8y + 11 &= -12\left(x + \frac{11}{4}\right)\end{aligned}$$

$$8y + 11 = -12x - 33$$

$$12x + 8y = -44$$

$$3x + 2y = -11$$

6. The feasible set is shown below.

