Enzyme Kinetics: The study of reaction rates. For the <u>one-way</u> I^{st} -order reaction: $S \rightarrow P$ the rate of reaction (V) is: $V = \frac{\Delta[P]}{\Delta t} = \frac{moles / L}{sec}$ For each very short segment dT of the reaction: $V = \frac{d[P]}{dt} = -\frac{d[S]}{dt} \approx \frac{\Delta P}{\Delta t}$ In a I^{st} -order reaction: $V = k_1[S]$ k_1 is a rate constant with units $1/s = s^{-1}$; V has units of moles per litre per second (mol L⁻¹s⁻¹).

In a reversible 1st-order reaction,

$$S \stackrel{k_1}{\longrightarrow} P$$
the net reaction rate V is
$$V = k_1[S] - k_{-1}[P]$$
At equilibrium, V = 0 and, $k_1[S]_{eq} = k_{-1}[P]_{eq}$ or
$$\frac{[P]_{eq}}{[S]_{eq}} = \frac{k_1}{k_{-1}} = K_{eq}$$









<u>Note</u>: V_{max} will be different for different [E]. We will now present an equation to describe this curve. It is based on the following mechanism: $E + S \stackrel{k_1}{\underset{k_{-1}}{\longrightarrow}} E \cdot S \stackrel{k_2}{\underset{k_{-2}}{\longrightarrow}} E + P$ k_1, k_{-1} etc. are rate constants. We define the Michaelis Constant $K_m \qquad \frac{k_{-1} + k_2}{k_1} = K_m$ $V_0 = \frac{k_2 [ES][S]}{[S] + \frac{k_{-1} + k_2}{k_1}}$

When the Enzyme is <u>saturated</u>, $[E S] = [E_{tot}]$ and $V_0 = V_{max} = k_2 [E_{tot}]$ This is the <u>Michaelis-Menton Equation</u>. It describes the relationship between V_0 and [S]; V_{max} and K_m are characteristics of particular enzymes. V_{max} is the maximum rate of reaction at a particular $[E_{tot}]$.



Recall that
$$K_m = \frac{k_{-1} + k_2}{k_1}$$
. Quite often $k_2 << k_{-1}$
So $K_m \approx \frac{k_{-1}}{k_1} = K_s = \frac{[E][S]}{[E \cdot S]}$

which is the equilibrium Enzyme-Substrate dissociation constant, a measure of the affinity of *S* for *E*.

$$E \cdot S \xrightarrow{k_{-1}} E + S$$

Big K_S or K_m means weak binding. Small K_S or K_m means strong binding.

One way to determine K_m and V_{max} is by non-linear least-squares fitting of the Michaelis-Menton equation to measured data.

Another way is a reciprocal plot of the MM equation.

The inverse of
$$V_0 = \frac{V_{\max}[S]}{[S] + K_m}$$
 is
 $\frac{1}{V_0} = \frac{K_m}{V_{\max}} \cdot \frac{1}{[S]} + \frac{1}{V_{\max}}$
 $Y = m \cdot X + b$
 $Slope = \frac{K_m}{V_{\max}}$ $Y - int ercept = \frac{1}{V_{\max}}$ $X - int ercept = -\frac{1}{K_m}$



$$V_{\text{max}} = k_2 [E_{tot}]$$
 and $\frac{V_{\text{max}}}{E_{tot}} = k_2 = k_{cat}$

So k_{cat} is an <i>E</i> -parameter that is independent of [<i>E</i>] and reports how fast an <i>E</i> works. <i>e.g.</i> At pH 7, 35°C carbonic anhydrase hydrates $4x10^5$ moles of CO ₂ yielding $4x10^5$ moles of HCO ₃ ⁻ per mole of enzyme per second – k_2 is a 1 st -order rate constant.	TABLE 5.1 Examples of catalytic constants	
	Enzyme	$k_{cat}(s^{-1})^*$
	Papain	10
	Ribonuclease	10 ²
	Carboxypeptidase	10 ²
	Trypsin	10 ² (to 10 ³)
	Acetylcholinesterase	10 ³
	Kinases	10 ³
	Dehydrogenases	10 ³
	Transaminases	10 ³
	Carbonic anhydrase	106
k_{cat} can be used for non-M-M	Superoxide dismutase	106
enzymes as well.	Catalase	107
	*The catalytic constants are given only as orders of magnitude. Table 5-1 Principles of Biochemistry, 4/e	

Since:
$$V_0 = \frac{k_{cat}[E_{tot}][S]}{[S] + K_m}$$
 when $[S]$ is $\langle K_m \ V_0 \cong \frac{k_{cat}[E_{tot}][S]}{K_m}$
 $\frac{k_{cat}}{K_m}$ is a 2^{nd} -order rate constant that measures how fast E and K_m S react.
The units are $\frac{litres}{moles \bullet \sec}$
The fastest that two molecules can diffuse together is about $10^9 - 10^{11} M^{-1} s^{-1}$ so this puts a limit on how fast the reaction can go.
 $\frac{k_{cat}}{K_m}$ ranges from 0.36 to 2.4 X $10^8 M^{-1} s^{-1}$.















So graphical analysis can give important information about the nature of the inhibitor and its mechanism of action.

Regulatory Enzymes

A metabolic pathway is one in which the product of the 1^{st} Enzyme is a substrate for the 2^{nd} Enzyme *etc*.



Often regulation occurs at the beginning of the path to prevent waste.

 E_1 is *Threonine dehydratase*. It is a key regulatory enzyme in the pathway and is inhibited by *L*-Ile.















 O_2 binding is also inhibited allosterically by 2,3-bisphosphoglycerate.

Because fetal hemoglobin has a lower affinity for BPG it has a higher affinity for O_2 . This permits the fetus to extract O_2 from the mother's blood.

Covalent Regulation

e.g. Glycogen phosphorylase is activated by phosphorylation of Ser.

This is reversible by a *phosphatase* that removes the phosphate.

Other possibilities: AMP, UMP, methyls, ADP ribose, sugars *etc*. can be added and removed.

In cancer cells, addition of N-acetyl-Glucose to Ser-529 of *phosphofructokinase-1* inhibits the enzyme slowing down glycolysis and speeding up the pentose phosphate pathway.

This permits cells to make more biosynthetic precursors and NADPH allowing faster growth. These changes permit much faster metabolic changes than are possible by gene regulation.

Irreversible Inhibitors

Usually they form a covalent bond with an active site AA.

e.g. Penicillin binds to the active site Ser in *transpeptidase*, an enzyme involved in bacterial cell wall synthesis.

e.g. Diisopropylfluorophosphate binds to Ser-195 in chymotrypsin.

<u>Zymogens</u>: Enzyme activation by proteolytic cleavage.

e.g. The pancreas produces inactive *trypsinogen*, *chymotrypsinogen*, *proelastase*, and *procarboxypeptidase* to prevent digestion of the pancreas.

In the gut, a duodenal enzyme *enteropeptidase* activates trypsin by removing AA 1-6 of *trypsinogen* producing active *trypsin*.

Then...

