

ERRATA

1. (Error noticed by Mitch Soivenski): **Page 4; the definition of transitivity:** Replace $(x,y) \in R$. by $(x,z) \in R$.
2. (Error noticed by Derek Krepski) **Page 22, Section 2.1, Exercise 6:** replace *min* by *max*.
3. **Page 80, Section 4.2, Exercise 9 (ii):** Change it to: Find a countable local basis at $[(0,0)]$, **or show such a local basis does not exist.**
4. **Page 83, Section 4.3, Exercise 5:** replace “the discrete sum $X_1 \oplus X_2$ ” by “the space X with the weak topology over $X_1 \cup X_2$ determined by $\{X_1, X_2\}$ ”.
5. **Page 118, Section 5.3, Exercise 5:** replace this exercise with the following:

6. **[revised].** Consider the set $X = \prod_{i \in \mathbb{R}} \mathbb{R}$ of all functions $\mathbb{R} \rightarrow \mathbb{R}$; let B the set of all bounded functions in X ; so $f \in B$ if there are numbers $u, v \in \mathbb{R}$, such that $u \leq f(x) \leq v$ for every $x \in \mathbb{R}$.

(a) Show that the sets of type $\prod_{i \in \mathbb{R}} (f(i) - \varepsilon(i), f(i) + \varepsilon(i))$, $f, \varepsilon \in B$, $\varepsilon(i) > 0$, comprise a basis for a topology \mathcal{T} over B . [Here $(f(i) - \varepsilon(i), f(i) + \varepsilon(i))$ denotes an interval; two simple basis sets are shown in Figure 2 (the functions that play the roles of ε are both constants in the illustration).]

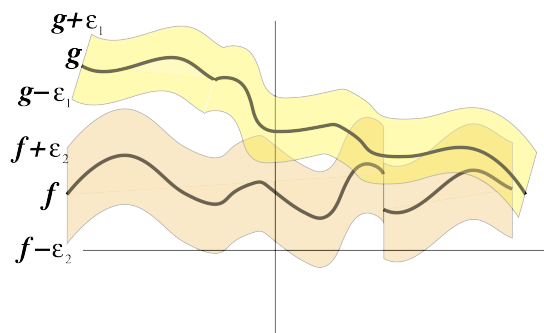


ILLUSTRATION. Two sets from our basis of bounded real valued functions. What is their intersection? Careful!

(b) Show that the topology \mathcal{T} is the subspace topology of the box topology over $X = \prod_{i \in \mathbb{R}} \mathbb{R}$.

(c) Define $\rho : B \times B \rightarrow \mathbb{R}$ by $\rho(f, g) = \sup\{|f(t) - g(t)| : t \in \mathbb{R}\}$. Show that ρ is a metric.

(d) Show that the topology \mathcal{T} is finer than the topology of the metric space (B, ρ) .

7. **Page 133, Section 6.2, Exercise 10:** The condition that f is onto is not needed.

8. **Page 163:** the proof of Theorem 4 has a gap: the open subset V of the intersection of the projections of the open sets in the skewer S (depicted in Illustration 7.6) does not necessarily satisfy $V \times Y \subset S$. An easy counterexample can be found even when S contains only one open set. To repair the proof start from the skewer S (Illustration 7.15) and use compactness to find a sub-skewer S' of S consisting of finitely many *basic* open sets (of type $U \times W$, $U \subset X$, $W \subset Y$. For the skewer S' the illustration 7.16 is fine and the rest of the argument is fine too.

9. (Error noticed by Ryan Sherbo) **Page 165, Exercise 7 (b):** the claim is false. Change 7 (b) to: Show that f open does not imply that f is continuous.

10. **Page 169, Section 7.3:**

Exercise 3(b): Change “closed subsets of X ” to “closed **nonempty** subsets of Y ”.

Exercise 5: Change “continuous” to “continuous **and onto**”.

11. **Page 173, Section 7.4, Exercise 5:** insert the word **Hausdorff** in front of the word BW-space.

12. **Page 178, Exercise 5:** replace ‘isomorphic’ by ‘homeomorphic’.

13. **Page 183, Exercise 1:** replace the first appearance of X_j by X_i .

14. **Page 187, the definition of regular space:** I would have rather stipulated that $x \notin F$, even though this follows from the rest of the definition.

15. **Page 190, Section 8.1, Exercise 3.** Change it to the following:

Let A and B be two disjoint subsets of a space X . Show that **if** there are U and V that separate A and B **then** $\{A, B\}$ is a separation of the subspace $A \cup B$ of X . **Show that the converse is false in general.**

16. **Page 194, Section 8.2, Exercise 9 (b):** Insert at the beginning of 9 (b) the sentence ‘**Let D be a countable dense subset of X ,**’ and replace $f(Y) = U_Y$ by $f(Y) = U_Y \cap D$.

17. (Error noticed by Lewis Robinson) **Page 200, line 6:** change $f_1(x)$ to $f_2(x)$.

18. (Error noticed by Lewis Robinson) **Page 230, line 1:** change $F : C \times I \rightarrow I$ to $F : C \times I \rightarrow C$.

19. (Error noticed by Lewis Robinson) **Page 251, line 10:** change $\cos 2\pi$ to $\cos 2\pi s$.

20. (Error noticed by Lewis Robinson) **Page 253, line 18:** change $c \leq 0$ to $c \geq 0$.
21. (Error noticed by Lewis Robinson) **Page 271, line 3 from the bottom:** change F to G .
22. (Error noticed by Lewis Robinson) **Page 317, line 7 from the bottom, spelling typo:** change ‘immerge’ to ‘emerge’.
23. **Pages 322-325:** To ensure that $\bigcap_{i=0}^{\infty} U_i \neq \emptyset$, so that we can choose the base point x in $\bigcap_{i=0}^{\infty} U_i$, modify the old sets U_i to $U_i \cup H$, where H is any half-space bounded to the left by a vertical plane Σ that is to the right of AHS.
24. (Error noticed by Lewis Robinson) **Page 334, line 2 from the top:** change $[c, d), (c, d]$ to $\varphi_k^{-1}([c, d)), \varphi_k^{-1}((c, d])$.
25. **Page 380:** the second appearance of f in the second line of the proof should be without a tilde over it. For what it’s worth, the tilde was inserted there by the typesetters between the proofreading #m and the proofreading #(m+1). I have not requested that, and there was no editing nearby.
26. (Error noticed by Lewis Robinson) **Page 400, line 2 from the bottom:** the word ‘continuous’ is redundant. Delete.
27. **Page 410, the second sentence of the part (a) of the proof of Proposition 3:** replace X with x , and add ‘containing y ’ at the end of the sentence.