

Answer key for the December 2005, Math 1300 final exam:

1. A: 4 equations, 2 variables, unique solution
B: 4 equations, 4 variables, infinitely solutions, 2 parameteers
C: 3 equations, 4 variables, no solutions

2. Determinant equals 8.

3. a) -4 , b) 2 , c) -1 , d) $A^{-1} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & -2 & 1 \end{bmatrix}$.

4. $z = -6$

5. $E_1 = \begin{bmatrix} 1 & 0 & 0 \\ 1 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$, $E_2 = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{bmatrix}$.

6. a) $(1, -1, -1)$, b) $\sqrt{6}$, c) 2 , d) $(\frac{2}{\sqrt{5}}, \frac{-1}{\sqrt{5}}, 0)$ and $(\frac{-2}{\sqrt{5}}, \frac{1}{\sqrt{5}}, 0)$, e) all \mathbf{x} with $2a - b = 0$.

7. a) point $(2, -1, 0)$, b) $(2, -3, -2)$, c) $2x - 3y - 2z - 7 = 0$.

8. a) W is a subspace, b) Basis: $\left\{ \begin{bmatrix} 0 & 1 \\ 0 & 0 \end{bmatrix}, \begin{bmatrix} 0 & 0 \\ 0 & 1 \end{bmatrix} \right\}$.

9. a) Yes, b) No: spanning set for \mathbb{R}^4 must have at least 4 vectors.

10. a) i. 3, ii. 3, iii. 3, iv. 4, v. 7, b) $\{ (1, -1, 0, -2, 0, 3), (0, 0, 1, 2, 5, -1) \}$,
c) $\{ (-2, 1, 0, 0, 0), (-3, 0, 1, 0, 0), (2, 0, 0, -3, 1) \}$.