

THE UNIVERSITY OF MANITOBA

DATE: February 24, 2005

Midterm Examination

DEPARTMENT & COURSE NO. 136.130

TITLE PAGE

EXAMINATION: Vector Geometry & Linear Algebra

TIME: 1 Hour

EXAMINER: see below

NAME: (Print in ink) \_\_\_\_\_

STUDENT NUMBER: \_\_\_\_\_

SIGNATURE: (in ink) \_\_\_\_\_

(I understand that cheating is a serious offense)

**Please indicate your instructor and section by placing a check mark in the appropriate box below.**

- Section L05     **V. Charette**     Tu, Th 10:00 am - 11:15 am     208 Armes
- Section L06     **N. Zorboska**     M, W, F 1:30 pm- 2:20 pm     204 Armes
- Section L07     **K. Doerksen**     M, W, F 1:30 pm- 2:20 pm     223 Wallace
- Section L08     **R.S.D. Thomas**     M, W, F 2:30 pm- 3:20 pm     208 Armes
- Section L09     **J. Sichler**     Tues. Evening     204 Armes
- Section L92     **Challenge for credit (SJR)**

**INSTRUCTIONS TO STUDENTS:**

This is a 1 hour exam. **Please show your work clearly.** Please justify your answers, unless otherwise stated.

No calculators or other aids are permitted.

This exam has a title page, 5 pages of questions and also 2 blank pages for rough work. Please check that you have all the pages.

The value of each question is indicated in the left-hand margin beside the statement of the question. The total value of all questions is 60.

**Answer all questions on the exam paper** in the space provide beneath the question. If you need more room, you may continue your work on the reverse side of the page, but **CLEARLY INDICATE** that your work is continued.

**DO NOT WRITE IN THIS COLUMN**

1. \_\_\_\_\_ /12

2. \_\_\_\_\_ /6

3. \_\_\_\_\_ /9

4. \_\_\_\_\_ /4

5. \_\_\_\_\_ /7

6. \_\_\_\_\_ /11

7. \_\_\_\_\_ /11

**TOTAL**

\_\_\_\_\_ /60

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**(12)** 1. Solve the following system by Gauss-Jordan elimination:

$$3x_1 + 6x_2 - 3x_4 = 0$$

$$2x_1 + 4x_2 + x_3 + x_4 = 0$$

$$x_1 + 2x_2 - x_3 + 4x_4 = 0$$

No marks will be given for any other method.

(6) 2. a) Find the determinant of  $M = \begin{bmatrix} -2 & \sqrt{3} & 4 \\ 0 & 1 & 0 \\ 0 & 0 & 5 \end{bmatrix}$ .

b) Suppose  $A$  is a  $3 \times 3$  matrix that is **invertible**, and that it can be put into row-echelon form by the following sequence of elementary row operations:

- 1) add  $\sqrt{2}$  times row 1 to row 2;
- 2) permute rows 2 and 3;
- 3) multiply row 3 by  $\sqrt{5}$ .

Find the determinant of  $A$ .

(9) 3. Let  $A = \begin{bmatrix} 1 & 2 \\ 2 & 1 \end{bmatrix}$ . Express  $A^{-1}$  as an explicit product of elementary matrices.

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(4) 4. Let  $A$ ,  $B$  and  $C$  be  $n \times n$  matrices and suppose that  $2AB - 3AC = I_n$ . Indicate how you can tell that  $A^{-1}$  exists, and find  $A^{-1}$  in terms of  $B$  and  $C$ .

(7) 5. Let  $X = [x_{ij}]$  be a  $2 \times 2$  matrix. Given that  $X + X^T = 0$  and  $x_{12} = 7$ , find  $X$ .

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**(11)** 6. Find the inverse of the following matrix by row reduction:

$$\begin{bmatrix} 2 & 0 & 1 \\ -2 & 1 & 0 \\ -2 & 0 & 1 \end{bmatrix}$$

No marks will be given for any other method.

(11) 7. Let  $A = \begin{bmatrix} 2 & 2 & 0 \\ 2 & 0 & 2 \\ -2 & 2 & 2 \end{bmatrix}$ . The adjoint of  $A$  is partially computed as shown. Enter the

two missing numbers in the boxes.

$$\text{Adj } A = \begin{bmatrix} -4 & -4 & \square \\ \square & -4 & -4 \\ 4 & -8 & -4 \end{bmatrix}.$$

Find  $\det A$ . Find  $A^{-1}$ .