

Find the derivative of each of the following functions by using the quotient rule.

1.  $\frac{\sqrt[11]{x}}{(5x^2 + 12x + 1)}$

16.  $\frac{\ln(x)}{(x^3 + 15)}$

31.  $\frac{\sqrt[11]{x}}{(x^3 + 15)}$

46.  $\frac{\sqrt[3]{x}}{e^x}$

2.  $\frac{\log_{12}(x)}{\sqrt{x}}$

17.  $\frac{(-\sin(x))}{\ln(x)}$

32.  $\frac{x^{2008}}{\tan(x)}$

47.  $\frac{\sqrt[12]{x}}{(-22x + 8)}$

3.  $\frac{e^x}{(x^3 + 15)}$

18.  $\frac{(-\cos(x))}{(11x^3)}$

33.  $\frac{\cot(x)}{(-22x + 8)}$

48.  $\frac{x^{100}}{\tan(x)}$

4.  $\frac{\sqrt[12]{x}}{\cot(x)}$

19.  $\frac{x^{31}}{(-\sin(x))}$

34.  $\frac{\log_{12}(x)}{\sqrt[14]{x}}$

49.  $\frac{\log_{12}(x)}{(-\cos(x))}$

5.  $\frac{\ln(x)}{(-22x + 8)}$

20.  $\frac{x^{2008}}{\sec(x)}$

35.  $\frac{\sqrt[3]{x}}{10^x}$

50.  $\frac{x^{31}}{(x^3 + 15)}$

6.  $\frac{\tan(x)}{\sqrt{x}}$

21.  $\frac{\sqrt{x}}{\tan(x)}$

36.  $\frac{\log_{12}(x)}{\left(\frac{1}{x}\right)}$

51.  $\frac{\sqrt[3]{x}}{(-\sin(x))}$

7.  $\frac{\tan(x)}{(x^3 + 15)}$

22.  $\frac{x^{2008}}{(-22x + 8)}$

37.  $\frac{\cot(x)}{\sqrt[14]{x}}$

52.  $\frac{\tan(x)}{\cot(x)}$

8.  $\frac{\cos(x)}{\cot(x)}$

23.  $\frac{\sin(x)}{\ln(x)}$

38.  $\frac{x^{2008}}{\sin(x)}$

53.  $\frac{\sqrt[12]{x}}{(-\cos(x))}$

9.  $\frac{x^{31}}{\cos(x)}$

24.  $\frac{\sqrt[11]{x}}{\csc(x)}$

39.  $\frac{e^x}{\csc(x)}$

54.  $\frac{2^x}{(11x^3)}$

10.  $\frac{(-\sin(x))}{(5x^2 + 12x + 1)}$

25.  $\frac{\sqrt[3]{x}}{\cos(x)}$

40.  $\frac{\cot(x)}{e^x}$

55.  $\frac{x^{100}}{\sec(x)}$

11.  $\frac{e^x}{(-\cos(x))}$

26.  $\frac{\ln(x)}{(-\cos(x))}$

41.  $\frac{\sqrt{x}}{(x^3 + 15)}$

56.  $\frac{\log_{12}(x)}{(-22x + 8)}$

12.  $\frac{x^{100}}{\cot(x)}$

27.  $\frac{\log_{12}(x)}{\ln(x)}$

42.  $\frac{2^x}{\csc(x)}$

57.  $\frac{\sqrt[12]{x}}{\sqrt{x}}$

13.  $\frac{\ln(x)}{\sqrt[14]{x}}$

28.  $\frac{\sin(x)}{(11x^3)}$

43.  $\frac{x^{31}}{10^x}$

58.  $\frac{\ln(x)}{\cot(x)}$

14.  $\frac{2^x}{(5x^2 + 12x + 1)}$

29.  $\frac{x^{2008}}{(x^3 + 15)}$

44.  $\frac{(-\cos(x))}{(-22x + 8)}$

59.  $\frac{2^x}{(-22x + 8)}$

15.  $\frac{e^x}{(11x^3)}$

30.  $\frac{\sqrt[3]{x}}{\ln(x)}$

45.  $\frac{\log_{12}(x)}{(11x^3)}$

60.  $\frac{\sqrt[12]{x}}{(5x^2 + 12x + 1)}$

Solutions:

$$1. \frac{(5x^2 + 12x + 1) \left( \frac{1}{11\sqrt[11]{x^{10}}} \right) - \sqrt[11]{x}(10x + 12)}{(5x^2 + 12x + 1)^2}$$

$$2. \frac{\sqrt{x} \frac{1}{x \ln 12} - \log_{12}(x) \frac{1}{2\sqrt{x}}}{(\sqrt{x})^2}$$

$$3. \frac{(x^3 + 15)e^x - e^x(3x^2)}{(x^3 + 15)^2}$$

$$4. \frac{\cot(x) \left( \frac{1}{12\sqrt[12]{x^{11}}} \right) - \sqrt[12]{x}(-\csc^2(x))}{(\cot(x))^2}$$

$$5. \frac{(-22x + 8) \frac{1}{x} - \ln(x)(-22)}{(-22x + 8)^2}$$

$$6. \frac{\sqrt{x} \sec^2(x) - \tan(x) \frac{1}{2\sqrt{x}}}{(\sqrt{x})^2}$$

$$7. \frac{(x^3 + 15) \sec^2(x) - \tan(x)(3x^2)}{(x^3 + 15)^2}$$

$$8. \frac{\cot(x)(-\sin(x)) - \cos(x)(-\csc^2(x))}{(\cot(x))^2}$$

$$9. \frac{\cos(x)(31x^{30}) - x^{31}(-\sin(x))}{(\cos(x))^2}$$

$$10. \frac{(5x^2 + 12x + 1)(-\cos(x)) - (-\sin(x))(10x + 12)}{(5x^2 + 12x + 1)^2}$$

$$11. \frac{(-\cos(x))e^x - e^x \sin(x)}{(-\cos(x))^2}$$

$$12. \frac{\cot(x)(100x^{99}) - x^{100}(-\csc^2(x))}{(\cot(x))^2}$$

$$13. \frac{\sqrt[14]{x} \frac{1}{x} - \ln(x) \left( \frac{1}{14\sqrt[14]{x^{13}}} \right)}{(\sqrt[14]{x})^2}$$

$$14. \frac{(5x^2 + 12x + 1)2^x(\ln 2) - 2^x(10x + 12)}{(5x^2 + 12x + 1)^2}$$

$$15. \frac{(11x^3)e^x - e^x(33x^2)}{(11x^3)^2}$$

$$16. \frac{(x^3 + 15) \frac{1}{x} - \ln(x)(3x^2)}{(x^3 + 15)^2}$$

$$17. \frac{\ln(x)(-\cos(x)) - (-\sin(x)) \frac{1}{x}}{(\ln(x))^2}$$

$$18. \frac{(11x^3)\sin(x) - (-\cos(x))(33x^2)}{(11x^3)^2}$$

$$19. \frac{(-\sin(x))(31x^{30}) - x^{31}(-\cos(x))}{(-\sin(x))^2}$$

$$20. \frac{\sec(x)(2008x^{2007}) - x^{2008}\sec(x)\tan(x)}{(\sec(x))^2}$$

$$21. \frac{\tan(x) \left( \frac{1}{2\sqrt{x}} \right) - \sqrt{x}\sec^2(x)}{(\tan(x))^2}$$

$$22. \frac{(-22x + 8)(2008x^{2007}) - x^{2008}(-22)}{(-22x + 8)^2}$$

$$23. \frac{\ln(x)\cos(x) - \sin(x) \frac{1}{x}}{(\ln(x))^2}$$

$$24. \frac{\csc(x) \left( \frac{1}{11\sqrt[11]{x^{10}}} \right) - \sqrt[11]{x}(-\csc(x)\cot(x))}{(\csc(x))^2}$$

$$25. \frac{\cos(x) \left( \frac{1}{3\sqrt[3]{x^2}} \right) - \sqrt[3]{x}(-\sin(x))}{(\cos(x))^2}$$

$$26. \frac{(-\cos(x)) \frac{1}{x} - \ln(x)\sin(x)}{(-\cos(x))^2}$$

$$27. \frac{\ln(x) \frac{1}{x \ln 12} - \log_{12}(x) \frac{1}{x}}{(\ln(x))^2}$$

$$28. \frac{(11x^3)\cos(x) - \sin(x)(33x^2)}{(11x^3)^2}$$

$$29. \frac{(x^3 + 15)(2008x^{2007}) - x^{2008}(3x^2)}{(x^3 + 15)^2}$$

$$30. \frac{\ln(x) \left( \frac{1}{3\sqrt[3]{x^2}} \right) - \sqrt[3]{x} \frac{1}{x}}{(\ln(x))^2}$$

$$31. \frac{(x^3 + 15) \left( \frac{1}{11\sqrt[11]{x^{10}}} \right) - \sqrt[11]{x}(3x^2)}{(x^3 + 15)^2}$$

$$32. \frac{\tan(x)(2008x^{2007}) - x^{2008}\sec^2(x)}{(\tan(x))^2}$$

$$33. \frac{(-22x + 8)(-\csc^2(x)) - \cot(x)(-22)}{(-22x + 8)^2}$$

$$34. \frac{\sqrt[14]{x} \frac{1}{x \ln 12} - \log_{12}(x) \left( \frac{1}{14\sqrt[14]{x^{13}}} \right)}{(\sqrt[14]{x})^2}$$

$$35. \frac{10^x \left( \frac{1}{3\sqrt[3]{x^2}} \right) - \sqrt[3]{x}(10^x)(\ln 10)}{(10^x)^2}$$

$$36. \frac{\left( \frac{1}{x} \right) \frac{1}{x \ln 12} - \log_{12}(x) \left( \frac{-1}{x^2} \right)}{\left( \frac{1}{x} \right)^2}$$

$$37. \frac{\sqrt[14]{x}(-\csc^2(x)) - \cot(x) \left( \frac{1}{14\sqrt[14]{x^{13}}} \right)}{(\sqrt[14]{x})^2}$$

$$38. \frac{\sin(x)(2008x^{2007}) - x^{2008}\cos(x)}{(\sin(x))^2}$$

39. 
$$\frac{\csc(x)e^x - e^x(-\csc(x)\cot(x))}{(\csc(x))^2}$$

40. 
$$\frac{e^x(-\csc^2(x)) - \cot(x)e^x}{(e^x)^2}$$

41. 
$$\frac{(x^3 + 15)\left(\frac{1}{2\sqrt{x}}\right) - \sqrt{x}(3x^2)}{(x^3 + 15)^2}$$

42. 
$$\frac{\csc(x)2^x(\ln 2) - 2^x(-\csc(x)\cot(x))}{(\csc(x))^2}$$

43. 
$$\frac{10^x(31x^{30}) - x^{31}(10^x)(\ln 10)}{(10^x)^2}$$

44. 
$$\frac{(-22x + 8)\sin(x) - (-\cos(x))(-22)}{(-22x + 8)^2}$$

45. 
$$\frac{(11x^3)\frac{1}{x\ln 12} - \log_{12}(x)(33x^2)}{(11x^3)^2}$$

46. 
$$\frac{e^x\left(\frac{1}{3\sqrt[3]{x^2}}\right) - \sqrt[3]{x}e^x}{(e^x)^2}$$

47. 
$$\frac{(-22x + 8)\left(\frac{1}{12\sqrt[12]{x^{11}}}\right) - \sqrt[12]{x}(-22)}{(-22x + 8)^2}$$

48. 
$$\frac{\tan(x)(100x^{99}) - x^{100}\sec^2(x)}{(\tan(x))^2}$$

49. 
$$\frac{(-\cos(x))\frac{1}{x\ln 12} - \log_{12}(x)\sin(x)}{(-\cos(x))^2}$$

50. 
$$\frac{(x^3 + 15)(31x^{30}) - x^{31}(3x^2)}{(x^3 + 15)^2}$$

51. 
$$\frac{(-\sin(x))\left(\frac{1}{3\sqrt[3]{x^2}}\right) - \sqrt[3]{x}(-\cos(x))}{(-\sin(x))^2}$$

52. 
$$\frac{\cot(x)\sec^2(x) - \tan(x)(-\csc^2(x))}{(\cot(x))^2}$$

53. 
$$\frac{(-\cos(x))\left(\frac{1}{12\sqrt[12]{x^{11}}}\right) - \sqrt[12]{x}\sin(x)}{(-\cos(x))^2}$$

54. 
$$\frac{(11x^3)2^x(\ln 2) - 2^x(33x^2)}{(11x^3)^2}$$

55. 
$$\frac{\sec(x)(100x^{99}) - x^{100}\sec(x)\tan(x)}{(\sec(x))^2}$$

56. 
$$\frac{(-22x + 8)\frac{1}{x\ln 12} - \log_{12}(x)(-22)}{(-22x + 8)^2}$$

57. 
$$\frac{\sqrt{x}\left(\frac{1}{12\sqrt[12]{x^{11}}}\right) - \sqrt[12]{x}\frac{1}{2\sqrt{x}}}{(\sqrt{x})^2}$$

58. 
$$\frac{\cot(x)\frac{1}{x} - \ln(x)(-\csc^2(x))}{(\cot(x))^2}$$

59. 
$$\frac{(-22x + 8)2^x(\ln 2) - 2^x(-22)}{(-22x + 8)^2}$$

60. 
$$\frac{(5x^2 + 12x + 1)\left(\frac{1}{12\sqrt[12]{x^{11}}}\right) - \sqrt[12]{x}(10x + 12)}{(5x^2 + 12x + 1)^2}$$