DATE: March 14, 2016 COURSE: <u>MATH 2150</u>

NAME:

STUDENT # : \_\_\_\_\_

Q1 [10]	Q2 [10]	Q3 [10]	Q4 [10]	Q5 [10]	Total $[50]$

[10] 1. Find maximum and minimum values of the function f(x, y, z) = 3yover the curve of intersection of the plane z = 2x - y and the ellipsoid  $2x^2 + y^2 + z^2 = 12$ . **Hint**: Use Lagrange multipliers.

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[10] 2. Let  $f(x,y) = y + 3\sqrt{x^2 + y^2}$ . Evaluate the double integral  $\int \int_D f(x,y) dA$ where D is the region bounded by the y-axis and  $x = \sqrt{2y - y^2}$ .

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[10] 3. Find the area of the finite plane region bounded by the curves  $y = x^3$ ,  $y = 2x^3$ ,  $x = y^3$  and  $x = 3y^3$ .

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[10] 4. Let *D* be the region satisfying  $4x + y \ge 3$  and  $2x - y \ge 0$ . Determine whether the double integral  $\int \int_D \frac{1}{\sqrt{x^2 + y + 1}} dA$  converges or diverges. Explain your work.

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[10] 5. Set up but do not evaluate the six triple iterated integrals in Cartesian coordinates for the function f(x, y, z) over the region enclosed by the surfaces  $y = 1 - x^2$ , z = 0 and y = z.